Simulink® Control Design™ Getting Started Guide

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Simulink® Control Design™ Getting Started Guide

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Contents

[Product Overview](#page-6-0)

[Steady-State Operating Points](#page-8-0)

[Linearization](#page-16-0)

[3](#page-16-0)

[1](#page-6-0)

[PID Control Design](#page-34-0)

Product Overview

Simulink Control Design Product Description Linearize models and design control systems

Simulink Control Design lets you design and analyze control systems modeled in Simulink. You can automatically tune arbitrary SISO and MIMO control architectures, including PID controllers. PID autotuning can be deployed to embedded software for automatically computing PID gains in real time.

You can find operating points and compute exact linearizations of Simulink models at various operating conditions. Simulink Control Design provides tools that let you compute simulation-based frequency responses without modifying your model.

Key Features

- Automatic tuning of PID, gain-scheduled, and arbitrary SISO and MIMO control systems in Simulink
- PID autotuning algorithm deployable to embedded software
- Operating-point calculation (trimming) and model linearization
- Frequency response estimation from simulation data
- Batch linearization for varying parameters and operating points
- Numerical optimization of compensators to meet time-domain and frequency-domain requirements (with Simulink Design Optimization™)

Steady-State Operating Points

- • ["What Is a Steady-State Operating Point?" on page 2-2](#page-9-0)
- "Steady-State Operating Points (Trimming) From Specifications" on page 2-3
- • ["magball Simulink Model" on page 2-5](#page-12-0)

What Is a Steady-State Operating Point?

A *steady-state operating point* of a model, also called an equilibrium or *trim* condition, includes state variables that do not change with time.

A model can have several steady-state operating points. For example, a hanging damped pendulum has two steady-state operating points at which the pendulum position does not change with time. A *stable steady-state operating point* occurs when a pendulum hangs straight down. When the pendulum position deviates slightly, the pendulum always returns to equilibrium. In other words, small changes in the operating point do not cause the system to leave the region of good approximation around the equilibrium value.

An *unstable steady-state operating point* occurs when a pendulum points upward. As long as the pendulum points *exactly* upward, it remains in equilibrium. However, when the pendulum deviates slightly from this position, it swings downward and the operating point leaves the region around the equilibrium value.

When using optimization search to compute operating points for nonlinear systems, your initial guesses for the states and input levels must be near the desired operating point to ensure convergence.

When linearizing a model with multiple steady-state operating points, it is important to have the right operating point. For example, linearizing a pendulum model around the stable steady-state operating point produces a stable linear model, whereas linearizing around the unstable steady-state operating point produces an unstable linear model.

See Also

findop

More About

- "Compute Steady-State Operating Points"
- "Simulink Model States Included in Operating Point Object"
- "Steady-State Operating Points (Trimming) From Specifications^{*"*} on page 2-3
- "Find Operating Points at Simulation Snapshots"

Steady-State Operating Points (Trimming) From Specifications

You can compute a steady-state operating point of a Simulink model by specifying constraints on the model states, outputs, and inputs, and finding a model operating condition that satisfies these constraints. You can trim your model to meet any combination of state, input, or output specifications. Computing an operating point in this way is called *trimming*. For more information on steady-state operating points, see "About Operating Points".

You can trim your Simulink model:

- In the **Steady State Manager**. For an example, see "Compute Operating Points from Specifications Using Steady State Manager".
- At the command line. For more information, see "Compute Operating Points from Specifications at the Command Line".
- In the **Linear Analysis Tool**. For more information, see "Compute Operating Points from Specifications Using Linear Analysis Tool".

For more information on selecting a trimming tool, see "Compute Steady-State Operating Points".

For state specifications, you can constrain the values of model states to known values or ranges. You can also define bounds for the derivatives of states that are not at steady state. Using such constraints, you can trim derivatives to known nonzero values or specify derivative tolerances for states that cannot reach steady state. For an example that trims a model for state specifications, see "Compute Operating Points from Specifications Using Linear Analysis Tool".

You can constrain the values of any root-level input or output ports to known values or ranges. You can also add output specifications to signals in your Simulink model. For an example that adds an output specification in this way, see "Compute Operating Points" from Specifications Using Steady State Manager".

If your trimming is unsuccessful; that is, if the optimization search was unable to meet all of your specifications, determine the specifications that could not be met by validating your trimmed operating point against the original specifications. For more information, see "Validate Operating Point Against Specifications".

After trimming your model, you can:

- Linearize your model at the resulting operating point. For more information, see "Linearize at Trimmed Operating Point".
- Simulate your model at the resulting operating point. For more information, see "Simulate Simulink Model at Specific Operating Point".

See Also

Functions findop | findopOptions

Apps Linear Analysis Tool | **Steady State Manager**

More About

- "Compute Operating Points from Specifications at the Command Line"
- "Compute Operating Points from Specifications Using Steady State Manager"
- "Compute Operating Points from Specifications Using Linear Analysis Tool"

magball Simulink Model

The Simulink model magball includes the nonlinear Magnetic Ball Plant in a single-loop feedback system.

The Magnetic Ball Plant subsystem is shown in the following figure.

The Magnetic Ball Plant model represents an iron ball of mass *M*. This ball moves under the influence of the gravitational force*, Mg,* and an induced magnetic force, $\frac{\beta i^2}{h}$. The presence of the squared term in the induced magnetic force results in a nonlinear plant.

The inductor in the electric circuit, shown in the following figure, causes the induced magnetic force. This circuit also includes a voltage source and a resistor.

The following table describes the variables, parameters, differential equations, states, inputs, and outputs of the Magnetic Ball Plant subsystem.

See Also

More About

• "Steady-State Operating Points (Trimming) From Specifications" on page 2-3

Linearization

- • ["Applications of Linearization" on page 3-2](#page-17-0)
- • ["Open-Loop Response of Control System for Stability Margin Analysis" on page 3-3](#page-18-0)
- • ["Bode Response of Simulink Model" on page 3-7](#page-22-0)
- • ["watertank Simulink Model" on page 3-12](#page-27-0)
- • ["Trimming and Linearizing Simulink Models" on page 3-15](#page-30-0)

Applications of Linearization

Linearization is useful in model analysis and control design applications. After you linearize a Simulink model at a specific operating point, you can use your linear model to:

- Compute the Bode response of the Simulink model.
- Evaluate loop stability margins by computing open-loop response.
- Obtain linear state-space, transfer-function, or zero-pole-gain representation of the combined Simulink model that contains only linear blocks.
- Analyze and compare plant response near different operating points.
- Design linear controller

Classical control system analysis and design methodologies require linear, timeinvariant models. Simulink Control Design automatically linearizes the plant when you tune your compensator. See "Design Compensator Using Automated PID Tuning and Graphical Bode Design".

- Analyze closed-loop stability.
- Measure the size of resonances in frequency response by computing closed-loop linear model for control system.
- Generate controllers with reduced sensitivity to parameter variations and modeling errors (requires Robust Control Toolbox™).

Examples and How To

- • ["Open-Loop Response of Control System for Stability Margin Analysis" on page 3-3](#page-18-0)
- • ["Bode Response of Simulink Model" on page 3-7](#page-22-0)
- "Steady-State Operating Points (Trimming) From Specifications" on page 2-3

More About

"Linearize Nonlinear Models"

Open-Loop Response of Control System for Stability Margin Analysis

This example shows how to analyze the open-loop response of a control system using the Linear Analysis Tool.

This example shows how to compute a linear model of the combined controller-plant system without the effects of the feedback signal. You can analyze the resulting linear model using, for example, a Bode plot.

Open Simulink model.

```
sys = 'watertank';
open_system(sys)
```


The Water-Tank System block represents the plant in this control system and contains all of the system nonlinearities.

In the Simulink Editor, specify the portion of the model to linearize. For this example, specify the loop opening using open-loop output analysis point.

- **1** Right-click the PID Controller block input signal (the output of the Sum block), and select **Linear Analysis Points** > **Input Perturbation**.
- **2** Right-click the Water-Tank System output signal, and select **Linear Analysis Points** > **Open-loop Output**.

Annotations appear in the model indicating which signals are designated as analysis points.

Tip If you do not want to introduce changes to the Simulink model, you can specify the analysis points in the Linear Analysis Tool. For more information, see "Specify Portion of Model to Linearize in Linear Analysis Tool".

Open the Linear Analysis Tool for the model.

In the Simulink Editor, select **Analysis** > **Control Design** > **Linear Analysis**.

By default, the analysis points you specified in the model are selected for linearization, as displayed in the **Analysis I/Os** drop-down list.

To linearize the model using the specified analysis points and generate a Bode plot of the

linearized model, click **Bode**.

By default, the Linear Analysis Tool linearizes the model at the model initial conditions, as shown in the **Operating Point** drop-down list. For examples of linearizing a model at a different operating point, see "Linearize at Trimmed Operating Point" and "Linearize at Simulation Snapshot".

Tip To generate response types other than a Bode plot, click the corresponding button in the plot gallery.

To view the minimum stability margins for the model, right-click the Bode plot, and select **Characteristics** > **Minimum Stability Margins**.

The Bode plot displays the phase margin marker. To show a data tip that contains the phase margin value, click the marker.

For this system, the phase margin is 90 degrees at a crossover frequency of 0.4 rad/s.

Related Examples

- • ["Bode Response of Simulink Model" on page 3-7](#page-22-0)
- "Steady-State Operating Points (Trimming) From Specifications" on page 2-3

More About

- "Linearize Nonlinear Models"
- • ["watertank Simulink Model" on page 3-12](#page-27-0)

Bode Response of Simulink Model

This example shows how to linearize a Simulink model at the operating point specified in the model using the **Linear Analysis Tool**.

Open Simulink model.

mdl = 'watertank'; open_system(mdl)

The Water-Tank System block represents the plant in this control system and includes all of the system nonlinearities.

In the Simulink window, specify the portion of the model to linearize:

- **1** To specify the linearization input, right-click the output signal of the PID Controller block, and select **Linear Analysis Points** > **Input Perturbation**.
- **2** To specify the linearization output, right-click the output signal of the Water-Tank

System, and select **Linear Analysis Points** $> \frac{1}{4} \times$ **Open-loop Output**. An open-loop output point is an output measurement followed by a loop opening, which removes the effects of the feedback signal on the linearization without changing the model operating point.

When you add linear analysis points, the software adds markers at their respective locations in the model. For more information on the different types of analysis points, see "Specify Portion of Model to Linearize".

For more information on defining analysis points in a Simulink model, see "Specify" Portion of Model to Linearize in Simulink Model". Alternatively, if you do not want to introduce changes to the Simulink model, you can define analysis points using the Linear Analysis Tool. For more information, see "Specify Portion of Model to Linearize in Linear Analysis Tool".

To open the Linear Analysis Tool for the model, in the Simulink model window, select **Analysis** > **Control Design** > **Linear Analysis**.

To use the analysis points you defined in the Simulink model as linearization I/Os, on the **Linear Analysis** tab, in the **Analysis I/Os** drop-down list, leave Model I/Os selected.

For this example, use the model operating point for linearization. In the **Operating Point** drop-down list, leave Model Initial Condition selected.

To linearize the system and generate a response plot for analysis, in the **Linearize** section, click a response. For this example, to generate a Bode plot for the resulting linear

model, click **Bode**.

The software adds the linearized model, linsys1, to the **Linear Analysis Workspace** and generates a Bode plot for the model. Linsys1 is the linear model from the specified input to the specified output, computed at the default model operating point.

For more information on analyzing linear models, see "Analyze Results Using Linear Analysis Tool Response Plots".

You can also export the linearized model to the MATLAB® workspace. To do so, in the **Data Browser**, drag linsys1 from the **Linear Analysis Workspace** to the **MATLAB Workspace**.

See Also

More About

- "Linearize Nonlinear Models"
- • ["watertank Simulink Model" on page 3-12](#page-27-0)
- • ["Open-Loop Response of Control System for Stability Margin Analysis" on page 3-3](#page-18-0)
- "Steady-State Operating Points (Trimming) From Specifications" on page 2-3

watertank Simulink Model

The Simulink model watertank includes the nonlinear Water-Tank System plant and a PI controller in a single-loop feedback system.

The Water-Tank System is shown in the following figure.

Water enters the tank from the top at a rate proportional to the voltage, *V*, applied to the pump. The water leaves through an opening in the tank base at a rate that is proportional to the square root of the water height, *H*, in the tank. The presence of the square root in the water flow rate results in a nonlinear plant.

The following table describes the variables, parameters, differential equations, states, inputs, and outputs of the Water-Tank System.

Trimming and Linearizing Simulink Models

This example shows how to use Simulink Control Design from command line. The MATLAB functions available in Simulink Control Design software allow for the programmatic specification of the input and output points for the linearization of a model. Additionally, there are MATLAB functions to extract and specify (trimming) operating points for a linearization. This example introduces some of these commands by linearizing a water-tank feedback control system. An open loop linearized model of the watertank will be extracted at an operating point where the tank level is at $H = 10$. The following 3 steps linearize and analyze the water-tank model.

Step 1: Configuring Linearization Points

Open the model.

watertank

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The linearization points specify the inputs and outputs of a linearized model. To extract the open loop linearized model, add an input point at the output of the Controller block and an output point, with a loop opening, at the output of the Water-Tank System block.

Specify the input point.

```
watertank io(1)=linio('watertank/PID Controller',1,'input');
```
Specify the output point with a loop opening.

```
watertank_io(2)=linio('watertank/Water-Tank System',1,'openoutput');
```
The linearization points can then be set and viewed in the model.

```
setlinio('watertank',watertank_io);
watertank
```
Step 2: Computing and Specifying Operating Points

This next step involves finding an operating point of the Simulink model 'watertank' so that the level of the tank is at $H = 10$. One approach is to simulate the model then extract the operating point when the simulation is near the desired value. The command FINDOP will simulate a model and extract the operating points at times defined in the function call.

```
opsim = findop('watertank',10)
  Operating point for the Model watertank.
  (Time-Varying Components Evaluated at time t=10)
States: 
----------
(1.) watertank/PID Controller/Integrator/Continuous/Integrator
       x: 1.69 
(2.) watertank/Water-Tank System/H
       x: 10.1 
Inputs: None 
----------
```
In this operating point, H is not at the desired value of 10. However, you can use this operating point to initialize a search for the desired operating point where $H = 10$. An operating point specification object allows you to specify the desired value of $H = 10$.

Create an operating point specification object.

```
opspec = operspec('watertank');
```
Initialize the values of the states of the operating point specification with the ones in the operating point opsim.

```
opspec = initopspec(opspec,opsim);
```
The specified operating point can then be searched for (trimmed) using the FINDOP command.

```
opss = findop('watertank',opspec);
 Operating point search report:
---------------------------------
 Operating point search report for the Model watertank.
 (Time-Varying Components Evaluated at time t=10)
Operating point specifications were successfully met.
States: 
----------
(1.) watertank/PID Controller/Integrator/Continuous/Integrator
      x: 1.26 dx: 0 (0)
(2.) watertank/Water-Tank System/H
     x: 10 dx: -1.1e-14 (0)
Inputs: None 
----------
Outputs: None 
----------
```
Step 3: Linearizing and Analyzing the Model

You are now ready to linearize the plant model by using the LINEARIZE function.

```
sys = linearize('watertank',opss,watertank io);
```
The resulting model is a state space object that you can analyze using any of the tools in the Control System Toolbox software.

bode(sys);

Close the Simulink model.

bdclose('watertank')

PID Control Design

PID Controller Tuning in Simulink

This example shows how to automatically tune a PID Controller block using **PID Tuner**.

Introduction of the PID Tuner

PID Tuner provides a fast and widely applicable single-loop PID tuning method for the Simulink® PID Controller blocks. With this method, you can tune PID controller parameters to achieve a robust design with the desired response time.

A typical design workflow with the **PID Tuner** involves the following tasks:

(1) Launch the **PID Tuner**. When launching, the software automatically computes a linear plant model from the Simulink model and designs an initial controller.

(2) Tune the controller in the **PID Tuner** by manually adjusting design criteria in two design modes. The tuner computes PID parameters that robustly stabilize the system.

(3) Export the parameters of the designed controller back to the PID Controller block and verify controller performance in Simulink.

Open the Model

Open the engine speed control model with PID Controller block and take a few moments to explore it.

open_system('scdspeedctrlpidblock')

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Design Overview

In this example, you design a PI controller in an engine speed control loop. The goal of the design is to track the reference signal from a Simulink step block scdspeedctrlpidblock/Speed Reference. The design requirement are:

- Settling time under 5 seconds
- Zero steady-state error to the step reference input.

In this example, you stabilize the feedback loop and achieve good reference tracking performance by designing the PI controller scdspeedctrl/PID Controller in the **PID Tuner**.

Open PID Tuner

To launch the **PID Tuner**, double-click the PID Controller block to open its block dialog. In the **Main** tab, click **Tune**.

Initial PID Design

When the **PID Tuner** launches, the software computes a linearized plant model seen by the controller. The software automatically identifies the plant input and output, and uses the current operating point for the linearization. The plant can have any order and can have time delays.

The **PID Tuner** computes an initial PI controller to achieve a reasonable tradeoff between performance and robustness. By default, step reference tracking performance displays in the plot.

The following figure shows the **PID Tuner** dialog with the initial design:

Display PID Parameters

Click **Show parameters** to view controller parameters P and I, and a set of performance and robustness measurements. In this example, the initial PI controller design gives a settling time of 2 seconds, which meets the requirement.

Adjust PID Design in PID Tuner

The overshoot of the reference tracking response is about 7.5 percent. Since we still have some room before reaching the settling time limit, you could reduce the overshoot by increasing the response time. Move the response time slider to the left to increase the closed loop response time. Notice that when you adjust response time, the response plot and the controller parameters and performance measurements update.

The following figure shows an adjusted PID design with an overshoot of zero and a settling time of 4 seconds. The designed controller effectively becomes an integral-only controller.

Complete PID Design with Performance Trade-Off

In order to achieve zero overshoot while reducing the settling time below 2 seconds, you need to take advantage of both sliders. You need to make control response faster to reduce the settling time and increase the robustness to reduce the overshoot. For example, you can reduce the response time from 3.4 to 1.5 seconds and increase robustness from 0.6 to 0.72.

The following figure shows the closed-loop response with these settings:

Write Tuned Parameters to PID Controller Block

After you are happy with the controller performance on the linear plant model, you can test the design on the nonlinear model. To do this, click **Update Block** in the **PID Tuner**. This action writes the parameters back to the PID Controller block in the Simulink model.

The following figure shows the updated PID Controller block dialog:

Completed Design

The following figure shows the response of the closed-loop system:

The response shows that the new controller meets all the design requirements.

You can also use the **Control System Designer** to design the PID Controller block, when the PID Controller block belongs to a multi-loop design task. See the example "Single Loop Feedback/Prefilter Compensator Design".

```
bdclose('scdspeedctrlpidblock')
```
See Also

PID Tuner

More About

- "Tune PID Controller to Favor Reference Tracking or Disturbance Rejection"
- "Analyze Design in PID Tuner"